Mechanism of Tacrine Block at Adult Human Muscle Nicotinic Acetylcholine Receptors

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Abstract We used single-channel kinetic analysis to study the inhibitory effects of tacrine on human adult nicotinic receptors (nAChRs) transiently expressed in HEK 293 cells. Single channel recording from cell-attached patches revealed concentration- and voltage-dependent decreases in mean channel open probability produced by tacrine (IC_{50} 4.6 µM at −70 mV, 1.6 µM at −150 mV). Two main effects of tacrine were apparent in the open- and closed-time distributions. First, the mean channel open time decreased with increasing tacrine concentration in a voltage-dependent manner, strongly suggesting that tacrine acts as an open-channel blocker. Second, tacrine produced a new class of closings whose duration increased with increasing tacrine concentration. Concentration dependence of closed-times is not predicted by sequential models of channel block, suggesting that tacrine blocks the nAChR by an unusual mechanism. To probe tacrine’s mechanism of action we fitted a series of kinetic models to our data using maximum likelihood techniques. Models incorporating two tacrine binding sites in the open receptor channel gave dramatically improved fits to our data compared with the classic sequential model, which contains one site. Improved fits relative to the sequential model were also obtained with schemes incorporating a binding site in the closed channel, but only if it is assumed that the channel cannot gate with tacrine bound. Overall, the best description of our data was obtained with a model that combined two binding sites in the open channel with a single site in the closed state of the receptor.

Key words: kinetic analysis • open-channel block • single-channel recording • maximum likelihood
• anticholinesterase

Introduction

The nicotinic acetylcholine receptor (nAChR)* from adult mammalian muscle is a heteropentameric protein with the subunit composition 2α, β, δ, ε. Each of the subunits is structurally homologous, and consists of a large, extracellular NH2-terminal domain, four membrane spanning segments (M1-M4), and a large intracellular loop between M3 and M4. Contained within the nAChR complex are two binding sites for acetylcholine, which are located in the NH2-terminal domains of the subunits, and a centrally located cation selective channel (Arias, 1996).

Although atomic structural insight recently emerged for the NH2-terminal ligand binding domain via X-ray crystallography of an ACh binding protein (Brejc et al., 2001) and a mutagenesis-based model of the muscle receptor (Sine et al., 2002), our understanding of the transmembrane domains continues to rely on lower resolution cryoelectron microscopy studies (Miyazawa et al., 1999), site-directed mutagenesis, affinity labeling, and the substituted cysteine accessibility method (SCAM) (for review see Arias, 1996). Together, these techniques lead to a model of the receptor in which the subunits are arrayed around a central ion channel, with the lining of the channel formed largely by the M2 domains of each of the subunits, and perhaps, smaller contributions from the extracellular ends of the M1 segments. (Arias, 1996; Miyazawa et al., 1999)

The M2 domains are highly conserved amongst the subunits, meaning that the overall channel structure can be viewed as a series of rings, stacked one upon the other. Each ring consists of five homologous amino acids, one from each subunit. The secondary structure of these channel lining segments is thought to be α-helical but with a distinct “kink” part way along their length. At the apex of this kink in each subunit is a conserved leucine residue. In one current model of channel gating, the ring of bulky leucine residues projects into the channel and occludes ion flux when the channel complex is in the closed state. When agonists bind and the channel opens, the leucine residues swing out of the pore, allowing ions to pass (Unwin, 1995). An alternative model, derived from SCAM studies, holds that the
channel gate is ~10 residues more cytoplasmic than the conserved leucine ring (Wilson and Karlin, 1998).

The ion channel of the nAChR is the target of a diverse group of noncompetitive antagonists that have generally been classified as open channel blockers (for review see Arias, 1996). Open channel blockers inhibit receptor function by entering and physically plugging the open channel, thereby preventing ion flux. Because the binding site is accessible only when the channel has been activated, and is located within the membrane field, the actions of open channel blockers are use and voltage dependent. Photoactivatable open channel blockers (e.g., chlorpromazine) were instrumental in pinpointing residues that line the channel and hence in the identification of the M2 segments as the major structural components of the channel (Changeux, 1990; Arias, 1996). However, despite the historical importance of open channel blockers in structure–function studies, our knowledge of their sites and mechanisms of action is incomplete. In particular, there have been very few systematic investigations of the kinetics of open channel block at the single channel level.

In this study, we investigated the blocking mechanism of tacrine (9-aminol-1,2,3,4-tetrahydroacridine) at human adult nAChRs. Tacrine is used clinically to treat Alzheimer’s disease and is thought to exert its therapeutic effects via inhibition of acetylcholinesterase. However, at higher concentrations than those used in the clinic, tacrine has also been found to inhibit a wide range of other proteins, including K+ channels (Drexler et al., 2000), NMDA receptors (Hershkowitz and Roga- 1991; Vorobjev and Sharonova, 1994), voltage-gated Ca2+ channels (Dolezal et al., 1997), and muscarinic acetylcholine receptors (Perry et al., 1988; Kiefer-Day et al., 1991; Kojima and Onodera, 1998). Previous studies showed that tacrine is a noncompetitive antagonist of Torpedo electric organ nAChRs (Canti et al., 1998), and speculated that the mechanism of this inhibition may involve open channel block. In the present study, we used maximum likelihood techniques to fit a series of kinetic models to single channel data. Our results suggest that tacrine is an atypical open channel blocker and interacts with at least two sites within the open- and one in the closed-state of the receptor. Thus, there may be multiple binding sites for tacrine and structurally related compounds in the nAChR complex.

MATERIALS AND METHODS

Materials

Dulbecco’s modified Eagle’s medium (DMEM), penicillin, and streptomycin were purchased from Gibco BRL. Tacrine was purchased from RBI. All other materials were obtained from Sigma-Aldrich. [125]I-labeled α-bungarotoxin was obtained from Amersham Biosciences. The sources of the human nAChR subunits were as described previously (Ohno et al., 1996).

Cell Culture and Receptor Expression

Human embryonic kidney 293 (HEK 293) cells were maintained in culture at 37°C, 5% CO2 in DMEM containing 10% FCS, 50 IU/ml penicillin, and 50 µg/ml streptomycin. In all experiments, cells were transfected at ~90% confluency using calcium phosphate precipitation as previously described (Prince and Sine, 1996). For each 35-mm culture dish, 2.7 µg of α subunit DNA and 1.35 µg each of β, δ, and ε were used in the transfection mixture. A plasmid encoding fluorescent green protein (pGreen lantern) was also included (0.5 µg/35 mm plate) in the transfection mixture to allow identification of transfected cells under fluorescence optics. The culture medium was replaced with fresh medium 12–16 h after transfection, and the cells were maintained at 37°C for a further 24–48 h before recordings or binding studies were performed.

Patch-clamp Recording

Recordings were obtained from transfected HEK 293 cells in the cell-attached configuration at membrane potentials of −70, −110 or −150 mV, at a temperature of 23°C. The bath and pipette solutions contained KRH buffer: (in mM) KCl 142, NaCl 5.4, CaCl2 1.8, MgCl2 1.7, and HEPES 25, pH 7.4. The patch pipette also contained various concentrations of acetylcholine (ACh) and tacrine, as required.

Recordings were made using an Axopatch 200A amplifier at a bandwidth of 50 kHz. Data were digitized at 200 kHz using an ITC-16 analogue to digital interface and recorded directly to hard-disk using the program Acquire (Bruxton Instruments). Channel openings and closings were detected off-line by the half-amplitude criterion using the program TAC (Bruxton Instruments) at a final bandwidth of 10 kHz. Open- and closed-duration histograms of the idealized data were constructed using TACFit (Bruxton Instruments) and were fitted by the sums of exponential functions.

At the concentrations of ACh (6–300 µM) used in this study, channel openings group into clusters corresponding to activation episodes of single AChRs. The long closings that mark the boundaries of clusters correspond to periods when all channels in the patch are in a desensitized conformation. Data within clusters were identified and selected for maximum likelihood analysis as described previously (Prince and Sine, 1998a). For each recording, we calculated the mean open and closed durations within clusters (nopen, nclosed) and the mean probability that the channel was open within clusters of openings (open). Concentration-response curves for ACh were constructed using Popen values and were fitted using the following form of the Hill equation:

\[ P_{\text{open}} = \frac{M \cdot X^n}{X^n + EC_{50}^n}, \]  

where \( X \) represents the concentration of ACh, \( M \) is the fitted maximum \( P_{\text{open}}, EC_{50} \) is the concentration of ACh yielding 50% of maximal \( P_{\text{open}} \) and \( n \) is the Hill coefficient.

Tacrine inhibition curves were fitted using the following equation:

\[ P_{\text{open}} = M \left( 1 - \frac{X^n}{X^n + IC_{50}^n} \right), \]  

where \( X \) represents the concentration of tacrine, \( M \) is the \( P_{\text{open}} \) in the absence of tacrine, \( IC_{50} \) is the concentration of tacrine that yields a \( P_{\text{open}} \) of 50% of \( M \), and \( n \) is the Hill coefficient.

Maximum Likelihood Analysis

To determine the rate constants governing receptor activation and block by ACh, recordings obtained over a range of ACh con-
centrations (6–300 μM) were analyzed according to Scheme A (see Fig. 3) using the maximum interval likelihood (MIL) program developed by Qin et al. (1996). A dead-time of 22 μs was imposed on all recordings. The MIL program calculates the likelihood that a given kinetic scheme and set of rate constants gave rise to the experimental set of openings and closings. The program then systematically varies the rate constants to maximize the likelihood. Once the parameters in Scheme A had been established, recordings obtained with 100 μM ACh and 1–60 μM tacrine (data at 60 μM tacrine were included only at −70 mV) were analyzed according to mechanisms B-I (see Fig. 3), with the values of the parameters for activation and block of the receptor by ACh constrained to the values determined by fits to Scheme A in the absence of tacrine (see Table IV). Nested models (models derived from the same parent kinetic scheme) were compared using the likelihood ratio test (LRT) statistic (Rao, 1973): \[
\text{LRT} = 2(LL_1 - LL_2),
\]
where \( LL_1 \) and \( LL_2 \) are the log-likelihood values of the models being compared. \( \text{LRT} \) is distributed as \( \chi^2 \) with the degrees of freedom being the difference in the number of free parameters between the two models.

We also made a global comparison of all models using the asymptotic information criterion (AIC) (Akaike, 1974). The AIC provides a method of comparing nonnested models and is calculated thus:

\[
\text{AIC} = 2(n - LL),
\]
where \( n \) is the number of free parameters and \( LL \) is the log-likelihood value for the model under consideration. The model with the minimum AIC value is considered the best.

**Ligand Binding Assays**

48 h after transfection, the growth medium was removed and the HEK 293 cells were harvested by gentle agitation in phosphate-buffered saline containing 5 mM EDTA. The cells were centrifuged for 5 min at 1500 g and then resuspended in KRH buffer containing 30 mg/l BSA. Tacrine affinity was determined by competition against the initial rate of [125I]-labeled α-bungarotoxin binding (Prince and Sine, 1998b). In a separate set of experiments designed to test the possibility that tacrine could desensitize the receptor, cells were preincubated for 1 h with the required concentrations of tacrine and carbamylcholine before addition of [125I]-labeled α-bungarotoxin.

Nonspecific binding was determined in the presence of 10 mM carbamylcholine. Binding data were analyzed according to the following form of the Hill equation:

\[
1 - f_{occ} = 1 - \frac{X^n}{X^n + IC_{50}^n},
\]
where \( f_{occ} \) is the fractional occupancy of receptor by the competing ligand, \( X \) is the concentration of competing ligand, \( n \) is the Hill coefficient, and \( IC_{50} \) is the concentration of the competing ligand that yields 50% occupancy of the receptor. Nonlinear regression was performed using Prism 3.0 (GraphPad Software).

**Results**

**Ligand Binding Experiments**

To assess whether tacrine competes with ACh at the receptor agonist binding sites, we determined the affinity of tacrine by competition against the initial rate of [125I]-labeled α-bungarotoxin binding. Tacrine bound with an \( IC_{50} \) of 309 ± 30 μM and a Hill coefficient of 1 ± 0.1 (\( n = 3 \)) (Fig. 1A). As described below, ACh-induced currents are antagonized by much lower concentrations of tacrine, eliminating competitive antagonism as the primary mechanism for functional inhibition of the nAChR by tacrine.

In a separate series of binding experiments, we assessed whether tacrine could desensitize the nAChR by determining the affinity of carbamylcholine in the presence of varying concentrations of tacrine (Fig. 1B). No difference was seen in log \( IC_{50} \) values for carbamylcholine (\( P = 0.64 \) by one-way ANOVA), indicating that tacrine does not produce the increase in ACh affinity expected of a desensitizing agent (Sine and Taylor, 1982).

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**Figure 1.** (A) Steady-state binding of tacrine to nAChRs. The smooth curve is a fit of the Hill equation (Eq. 3) to the data with the following parameters: \( IC_{50} = 4.5 ± 0.7 \mu M \), \( n = 0.8 ± 0.1 \); 1 μM tacrine \( (\bigtriangleup) \) \( IC_{50} = 3.4 ± 0.4 \), \( n = 0.7 ± 0.1 \); 10 μM tacrine \( (\bigtriangledown) \) \( IC_{50} = 5.5 ± 0.7 \mu M \), \( n = 0.7 ± 0.1 \); 100 μM tacrine \( (\bigstar) \) \( IC_{50} = 6.1 ± 1 \mu M \), \( n = 1 ± 0.1 \). For both types of experiment, ligand affinity was determined by competition against the initial rate of [125I]-labeled α-bungarotoxin as described in MATERIALS AND METHODS. Each point is the mean of three determinations and the error bars represent the SEM.
Patch-Clamp Experiments: Initial Observations

Activation by ACh. We recorded responses to 6–300 μM ACh at three membrane potentials: −70, −110, and −150 mV. At each potential, periods of channel activity corresponding to the activation of single nAChRs were readily discernible as clusters of channel openings bounded by long closed times (Fig. 2). For each recording, we calculated the mean $P_{\text{open}}$ (probability that the channel is in the open state) within clusters and fitted the Hill equation to our data. The resulting concentration-response curves revealed Hill coefficients close to two at each potential and a voltage-dependent decrease in $EC_{50}$ (Fig. 2, Table I).

Within clusters, there were two main components in the closed time histogram. The faster component (∼20 μs) did not vary in duration, but increased in relative area with increased ACh concentration. In contrast, the longer component of intracluster closings (∼100 μs at 100 μM ACh) decreased in relative area with tacrine concentration but moved progressively to shorter durations. This component of the closed time histogram is described by a rate constant termed $\beta'$, (also known as effective channel opening rate) (Sine and Steinbach, 1987) and arises from dwells of the channel in the C, AC, and A2C states (Fig. 3, Scheme A).

The long closed times which bound clusters of openings are thought to represent periods when all receptors in the patch are desensitized. We observed three exponential components of desensitization closed times in this study. Long (∼7.5 s) duration closings were observed at all concentrations of ACh and were somewhat variable in duration. Desensitization on this time scale has been reported in numerous studies dating back to Katz and Thesleff (1957). Medium (∼30 ms) duration desensitization closings could be resolved at concentrations above 10 μM ACh, but were obscured by slower components of the closed time probability density function (p.d.f.) at lower concentrations of agonist. This type of desensitization was of constant duration across the concentration range 20–300 μM and is in good agreement with results from rapid agonist application experiments which have yielded desensitization time constants of 15–50 ms (Dilger and Liu, 1992; Franke et al., 1992; Jahn et al., 2001). A similar duration closed-time component was also observed by Sine and Steinbach (1987) in single channel recordings from BC3H-1 cells. Finally, at concentrations of 60 μM ACh and above we observed a fast (2 ms) desensitization component that did not alter in duration with agonist concentration. A similar (4.5 ms) component was noted by Zhang et al. (1995) and was assumed to represent a rapid form of desensitization.

Inhibition by tacrine. To determine the effects of tacrine on ACh-evoked single channel activity, we recorded responses to 100 μM ACh in the presence of 1–100 μM tacrine at membrane potentials of −70, −110 and −150 mV. We chose 100 μM ACh because it allowed clusters to be identified over a wide range of tacrine concentrations. Inclusion of tacrine in the patch pipette produced a concentration- and voltage-dependent reduction in channel open probability with fitted $IC_{50}$ values close to 3 μM (Fig. 4, Table II). In a separate series of experiments, we recorded responses to 300 μM ACh in the presence of 10 μM tacrine. As predicted for noncompetitive antagonism, the reduction in $P_{\text{open}}$ (expressed as percentage change from control) produced by 10 μM tacrine at 300 μM ACh (74%)
**Figure 3.** Kinetic schemes used in maximum likelihood fitting. (Notation used for receptor states) C, AC, A2C are closed states with agonist binding sites unoccupied, singly occupied, and doubly occupied, respectively; A2O is the open state; A2B is the open state blocked by acetylcholine; A2BT and A2BTT are distinct open-blocked states that have bound tacrine to one site within the channel; A2BTT is an open blocked state in which tacrine has bound to two sites within the channel; A2CT and A2CTT are closed states which have bound one and two molecules of tacrine respectively. (Notation used for rate constants) General mechanism. (A) $\beta$, $\alpha$ are channel opening and closing rate constants respectively; $k_{11001}^a, k_{11001}^b, k_B^a$ are association rate constants for ACh at the two agonist binding sites and channel block site respectively; $k_{11002}^a, k_{11002}^b, k_B^b$ are dissociation rate constants for ACh at the two agonist binding sites and channel block site respectively. A is the concentration of ACh. DB indicates that the scheme was constrained by detailed balancing. In general mechanisms B–I, only the rate constants that were derived by maximum likelihood fitting are shown. Other rate constants within the schemes were fixed to values determined from fitting to Scheme A (see Table IV).
fits are summarized in Table II. The top of each curve was fixed to the Hill equation (Eq. 2). The parameters derived from these fits are summarized in Table II. The top of each curve was fixed to the mean $P_{\text{open}}$ obtained in the absence of tacrine.

was essentially the same as that produced at 100 μM ACh (77%). To determine whether tacrine can act as an agonist at the nAChR we made recordings with 10 μM tacrine and no ACh in the patch pipette. No responses were observed in the presence of tacrine alone ($n = 3$).

Effects of Tacrine on Dwell-time Distributions

Preliminary examination of channel open- and closed-times revealed that tacrine decreased $m_{\text{open}}$ and increased $m_{\text{closed}}$. These effects are strongly suggestive of open channel block, which for the nAChR has been described classically by Scheme B1 (Fig. 3).

In Scheme B1 (Neher and Steinbach, 1978), the open-blocked state (A2BT) is connected only to the open state (A2O). This simple connectivity means that the rate constants $k_{+1}$ and $k_{-1}$ can be determined by examining the effects of blocker on the distributions of open, burst, and closed durations. As in most previous studies of nAChR channel block, therefore, Scheme B1 was our starting point from which to investigate the kinetics of block.

Open Time Distributions

More-detailed examination of the open-duration histograms (Fig. 5 A) revealed that the tacrine-induced decrease in mean channel open time was concentration and voltage dependent. Neglecting for the moment block of the channel by ACh itself, Scheme B1 predicts the reciprocal of the mean channel open duration ($\tau_{\text{open}}$) to be related linearly to the concentration of open channel blocker ($T$):

$$\frac{1}{\tau_{\text{open}}} = \alpha + T.k_{+1}.$$  (4)

To apply Eq. 4 to experimental data, it is first necessary to correct apparent mean open durations for unresolved dwells in the closed states. These missed closings result in the concatenation of successive channel openings and thus in an overestimation of $\tau_{\text{open}}$. In the present study, the exact form of Eq. 4 cannot be used because the partially resolved brief closings that arise from channel gating are of a similar duration to those that arise from block of the channel by ACh itself. However, it can be demonstrated (Appendix A) that open time correction can be omitted for our present data and that using the apparent mean open time ($\tau_{\text{app}}$), yields a straight-line with a slope approximating $k_{+1}$:

$$\frac{1}{\tau_{\text{app}}} = \frac{1}{\tau_{0}} + T.k_{+1}.$$  (5)

where $\tau_{0}$ is the apparent mean open time at zero tacrine concentration. Plots of Eq. 5 are shown in Fig. 5 B.

Burst-duration Distributions

An alternative method of investigating channel block is the integration method of Neher (1983). The integration method makes use of the fact that for sequential block, burst duration increases with blocker concentration, but the total open time per burst does not vary. On the other hand, “parallel block” models such as Scheme C2 (Fig. 3) that provide the receptor with a pathway back to the closed state, thereby bypassing the unblocked open state, predict a decrease in the total open time per burst. Therefore, in theory, the integration method can distinguish between sequential and parallel block mechanisms. However, a limitation of the integration method is that it can only be used when individual bursts can be identified unequivocally, i.e., at low concentrations of agonist where the mean duration of block closings is shorter than $1/\beta'$. In the present study, this condition cannot be met because even at the lowest concentrations of tacrine, the mean block duration is considerably longer than $1/\beta'$.

### TABLE II

<table>
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<tr>
<th>Membrane potential</th>
<th>$IC_{50}$</th>
<th>$n$</th>
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<tbody>
<tr>
<td>mV</td>
<td>μM</td>
<td></td>
</tr>
<tr>
<td>−70</td>
<td>4.6 ± 0.23</td>
<td>1.4 ± 0.08</td>
</tr>
<tr>
<td>−110</td>
<td>2.5 ± 0.24</td>
<td>1.5 ± 0.15</td>
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<tr>
<td>−150</td>
<td>1.6 ± 0.09</td>
<td>1.9 ± 0.19</td>
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The parameters and error estimates are derived from fits of Eq. 2 to the data shown in Fig. 2. Each fitted parameter is expressed ± SE. $IC_{50}$ is the concentration of tacrine that produces a 50% reduction in $P_{\text{open}}$. $n$ is the Hill coefficient.
Predictions about the closed time distribution can also be made from Scheme B1. First, open channel block should produce a new class of closings and these closings should increase in frequency with increasing blocker concentration. Ogden and Colquhoun (1985) exploited this predicted increase in “blocking frequency” to calculate blocker association rate constants. Blocking frequency ($B_f$) is simply the number of blocking events per unit time and is calculated thus:

$$B_f = \frac{N_{\text{block}}}{N_{\text{open}} \cdot m_{\text{open}}}.$$

where $N_{\text{block}}$ is the number of closings attributable to block by tacrine, $N_{\text{open}}$ is the number of channel openings (corrected for missed openings), and $m_{\text{open}}$ is the apparent mean channel open time. For blockers that follow Scheme B1, plots of $B_f$ against blocker concentration should be straight lines with slopes of $k_{T_{i,j}}$. As predicted by Scheme B1, tacrine produced an additional exponential component in the closed time distribution.
Kinetics of activation of the receptor by ACh. Detailed kinetic analysis of the mechanism by which tacrine inhibits the nAChR requires knowledge of the rate constants that govern activation of the receptor by ACh in the absence of tacrine. To estimate these rate constants we recorded time histograms (Fig. 5 C) that allowed us to fit a series of kinetic models to our single channel data using maximum likelihood techniques.

A final prediction of Scheme B1 is that the time constant of block closings should depend solely on the dissociation constant of the blocker ($k_{T,2}$) and thus should be concentration independent. Contrary to Scheme B1, however, the duration of block closings increased with increasing tacrine concentration (Fig. 5, A and D).

Taking our initial analyses of open and closed distributions together, our data strongly suggest that tacrine inhibits the nAChR by interacting with the open channel but the mechanism of this inhibition is incompatible with Scheme B1. To gain further insight into how tacrine interacts with the nAChR we therefore decided to fit a series of kinetic models to our single channel data using maximum likelihood techniques.

Maximum Likelihood Analysis

Kinetics of activation of the receptor by ACh. Detailed kinetic analysis of the mechanism by which tacrine inhibits the nAChR requires knowledge of the rate constants that govern activation of the receptor by ACh in the absence of tacrine. To estimate these rate constants we recorded currents at 6–300 μM ACh and analyzed the resulting open and closed dwell times using maximum likelihood fitting (MATERIALS AND METHODS). We used a standard linear scheme (Fig. 3, Scheme A) to describe activation of the receptor and block by ACh itself. Scheme A does not include moniligand openings of the receptor, but at the concentrations of ACh used in this series of experiments only a single class of openings was observed. Scheme A should therefore be a good approximation of reality under the conditions used in this study. A global set of rate constants (Table IV) for Scheme A was obtained by simultaneous fitting to data obtained over the range of ACh concentrations, and the resulting probability density functions are shown as smooth curves superimposed on the open and closed time histograms (Fig. 6). The rate constants derived from this series of experiments are, at −70 mV, very similar to those observed by Ohno et al. (1996). Our results reveal that the voltage dependence of the EC$_{50}$ of ACh is largely due to decreases in the channel closing rate (α) and the rates of dissociation of ACh from the agonist binding sites ($k_{−1}, k_{−2}$).

Parameters were derived from maximum likelihood fitting of Scheme A (Fig. 3) to single-channel data obtained at ACh concentrations from 6–300 nM and are expressed ± SE. The rate constants are defined in the legend to Fig. 3. Association rate constants are given in units of μM$^{-1}$ s$^{-1}$, and all others in units of s$^{-1}$. $K_1$, $K_2$, and $K_B$ (mM) are dissociation constants governing the binding of ACh to the high- and low-affinity agonist binding sites and the channel block site, respectively. $\Theta$ is the equilibrium constant governing channel opening. $K_1$, $K_2$, $K_B$, and $\Theta$ were calculated from their constituent rate constants.

Kinetics of tacrine inhibition. Once the parameters for channel activation by ACh were determined, we applied maximum likelihood fitting techniques to recordings made at 100 μM ACh in the presence of tacrine. We fitted 16 schemes to our data (Fig. 3), constraining the rate constants for activation and block of the nAChR by ACh to the values in Table IV. Global fitting was again performed by simultaneous fitting of data obtained over a range of tacrine concentrations.

First, we considered the classic sequential scheme for open channel block (Scheme B1). A priori, Scheme B1 cannot account for the inhibition of the nAChR by tacrine because it predicts that the durations of block closings should be independent of tacrine concentration. However, fitting Scheme B1 to our data provides a baseline for comparing the merits of other models. As expected, Scheme B1 yielded a poor fit to our data, particularly in the closed time distribution.

### Table III

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<tr>
<th>Membrane potential</th>
<th>Fit parameters for Apparent Open Time and Blocking Frequency Plots</th>
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<tr>
<td>−70 mV</td>
<td>$k_{T,1}$ (μM$^{-1}$ s$^{-1}$) 95 ± 2</td>
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<tr>
<td>−110 mV</td>
<td>100 ± 3</td>
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<td>−150 mV</td>
<td>114 ± 5</td>
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### Table IV

<table>
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<tr>
<th>kinetic parameters for ACh Activation of Human Adult nAChRs</th>
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<tr>
<td>$k_{T,1}$ 211 ± 11</td>
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<tr>
<td>$k_{T,2}$ 4,126 ± 260</td>
</tr>
<tr>
<td>$K_1$ 19.6</td>
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<tr>
<td>$K_2$ 165 ± 4</td>
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<tr>
<td>$K_B$ 20,261 ± 262</td>
</tr>
<tr>
<td>$\beta$ 53,211 ± 1,163</td>
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<tr>
<td>$\alpha$ 2,290 ± 49</td>
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<tr>
<td>$\Theta$ 32.2</td>
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<tr>
<td>$k_{−1,b}$ 38 ± 4</td>
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<td>$k_{−2,b}$ 149,000 ± 4,122</td>
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<td>$K_0$ 3,921</td>
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Next, we fitted a series of kinetic schemes to our data that described more complex interactions between tacrine and the receptor (Fig. 3). We considered three general mechanisms by which tacrine might bind to and inhibit the function of the nAChR: (a) competitive inhibition at the nAChR agonist binding sites; (b) binding to the closed channel; and (c) binding to the open channel. The individual schemes...
are described in detail in the discussion. However, the following general observations can be made by considering AIC ranking (Table V): (a) schemes that allowed tacrine to bind with the closed channel of the receptor produced an improved fit relative to the sequential scheme, but only if it was assumed that the channel could not open or close with tacrine bound (Schemes C4, G2); (b) improvements relative to the sequential model were also obtained with models that allowed tacrine to bind to the open channel but also allowed the channel to close with tacrine still bound (Schemes C5, G1); (c) schemes that postulated two binding sites for tacrine within the open channel of the receptor (Mechanisms E–I) yielded dramatic improvements in goodness of fit; (d) the best schemes had two binding sites in the open state and allowed interactions between tacrine and the closed state (Mechanisms G–I). Taking into account our results from maximum likelihood analysis and from single channel simulations (see below), the best overall description of our data is achieved with Scheme G2. Fig. 7 shows the predicted probability density functions for Scheme G2 superimposed over our experimental data.

Based on the fitted rate constants for Scheme G2, several predictions can be made about the kinetic behavior of the nAChR channel in the presence of tacrine. For the open time distribution, predictions of Scheme G2 are relatively straightforward. In any kinetic scheme, the lifetime of a particular state depends on the sum of the rate constants governing exit from that state. Thus, Scheme G2 predicts that the reciprocal mean open time of the channel ($\tau_{open}$) varies linearly with tacrine concentration as follows:

$$\frac{1}{\tau_{open}} = \alpha + T \cdot k_{T+1},$$

(7)

where $\alpha$ is the channel closing rate, $T$ is the concentration of tacrine and $k_{T+1}$ is the association rate for tacrine. Eq. 7 has the same form as Eq. 5 and comparing the $k_{T+1}$ values in Table VI with the values of $k_{T+1}$ derived from apparent open time plots (Table III) demonstrates excellent agreement between experimental and predicted association rates.

For the closed time distribution, the situation is more complicated because of intercommunication between the open-blocked states with one and two bound tacrines, and between the closed-blocked state and the closed states of the receptor. Considering first the open-blocked states, it is clear that any given channel-block event might consist solely of a dwell in the mono-ligated $A_2B_T$ state followed by dissociation of tacrine and return to the open state. Alternatively, it might consist of a dwell in $A_2B_{TT}$ followed by multiple transitions to $A_2B_{TT}$ before return to the open state. These two types of block events are predicted to give rise to two exponential components in the closed-time distribution, but the rate constants describing these exponentials do not relate directly to the lifetime of any individual states in Scheme G2. As described by Colquhoun and Hawkes (1981, 1995), the rate constants ($\lambda_1$, $\lambda_2$) of these exponentials must be calculated by solving the quadratic equation $\lambda^2 + b\lambda + c = 0$, where:

$$-b = \lambda_1 + \lambda_2 = k_{T-1} + k_{T+2} \cdot k_{T-2}$$

and

$$c = \lambda_1 \cdot \lambda_2 = k_{T-1} \cdot k_{T-2}.$$

Similarly, the relative areas ($a_1, a_2$) of the two components are given by the formulæ:

$$a_1 = \frac{k_{T-1} \cdot (k_{T-2} - \lambda_1)}{\lambda_1 \cdot (\lambda_2 - \lambda_1)}$$

and

$$a_2 = 1 - a_1.$$

The derivations of these equations are given in full in Appendix B. As shown in Fig. 8, Scheme G2 predicts that the component of the closed-time distribution described by $\lambda_1$ becomes briefer and that its relative area ($a_1$) decreases as the concentration of tacrine is increased. However, we could not identify this closed-time component in our experimental data, probably due to temporal overlap of the $\lambda_1$ component with closings arising from agonist binding and channel gating ($\beta'$). Conversely, Scheme G2 predicts that the component of the closed-time component described by $\lambda_2$, increases in duration and relative area ($a_2$) with increasing tacrine concentration. The time constants of these closings are in excellent agreement with our experimental data (Fig. 8).
Figure 7. Kinetics of activation of nAChRs by 100 μM acetylcholine in the presence of the indicated concentrations of tacrine. Left panels show traces of individual clusters from patches displayed at a bandwidth of 5 kHz. The smooth curves through the open and closed time histograms are theoretical probability density functions calculated from the fitted rate constants for Scheme G2, with parameter values given in Table VI. At each concentration of tacrine, the number of clusters analyzed ranged as follows: −70 mV 44–127, −110 mV 50–136, −150 mV 51–88, whereas the number of events ranged from 4,932–11,580 (−70 mV), 6,020–12,940 (−110 mV) and 3,140–11,904 (−150 mV).
For the closed-blocked state $A_2CT$, the situation is even more complex. In Scheme A, which describes receptor activation in the absence of tacrine, the receptor may shuttle between the C, AC, and $A_2C$ states a number of times before finally opening. In the closed-time histogram this is reflected in an exponential component whose time constant, $\beta'$ (the effective channel opening rate), depends on the values of $k_{T1}$, $k_{T2}$, $k_{T3}$, $k_{T4}$, $k_{T5}$, and the concentration of ACh. In Scheme G2, $A_2CT$ is directly linked to $A_2C$ and thus indirectly to AC and C, predicting that closed channel block should affect the $\beta'$ component in a manner that depends on tacrine concentration. This concentration dependence arises because increasing concentrations of tacrine progressively trap the receptor in transitions between the $A_2CT$ and $A_2C$ states. The probability that a receptor in the $A_2C$ state binds tacrine, as opposed to opening or losing a molecule of ACh, can be calculated thus:

$$P = \frac{k_{T+3} \cdot T}{\beta + k_{-2} + k_{T+3}}.$$

At 60 $\mu$M tacrine ($-70$ mV) $P = 0.11$, suggesting that even at the maximum concentrations of tacrine examined in this study, only marginal changes in $\beta'$ should be observed. In agreement with this prediction we found no tacrine-dependent changes in the value of $\beta'$ in our experimental data.

A somewhat unexpected finding in our initial analysis was that the tacrine association rates predicted by the blocking frequency were consistently slower than those derived from apparent open time plots. In contrast, previous studies have demonstrated that these methods yield essentially identical results (Ogden and Colquhoun, 1985). To understand these findings in the context of Scheme G2, it is important to realize that while blocking frequency and apparent open time plots are both used to derive the same parameter ($k_{T1}$), they make use of very different information. In the apparent open time plot we measure interruption of channel openings by blocking events. Providing these block closings are long enough to be resolved, they will shorten the mean channel open time whether they fol-
low a single- or multiple-component distribution. Apparent open time plots are therefore a robust method for deriving values of $kT_1$. By contrast, the blocking frequency plot requires us to determine the number of block-closings. This can be a problem for mechanisms that yield multicomponent and/or concentration-dependent distributions of block closings. As detailed above, the distribution of block closings predicted by Scheme G2 is described by two exponential functions. One component increases in mean duration and relative area with increasing tacrine concentration, and because this is the only clearly identifiable new component in the closed-time histogram, only closings from this exponential contribute to the block frequency plot. The second exponential component becomes briefer and has a smaller area as the concentration of tacrine increases. This component cannot be identified in the closed-time histogram because it becomes submerged beneath the exponential components that arise from channel gating and agonist binding. Neglect of the brief block exponential, which at 60 $\mu$M ACh ($-70$ mV) still comprises $\sim$10% of all block closings, therefore leads to an underestimation of blocking frequency and hence $kT_1$.

Effects of Tacrine on Cluster Duration

To allow data to be analyzed using the MIL program, clusters of channel openings corresponding to the activation of single channels must be identified. Our procedure involves selecting groups of openings bounded by long closed times that correspond to periods when all channels in the patch are desensitized. In the absence of tacrine, responses to 100 $\mu$M ACh at $-70$ mV (Fig. 5) revealed three distinct components of closings attributable to desensitization: fast $\tau_{d1} 2.2 \pm 0.8$ ms, 1.1 $\pm$ 0.3% total closings; medium $\tau_{d2} 30 \pm 7$ ms, 0.7 $\pm$ 0.2% total closings; and slow $\tau_{d3} 7.400 \pm 3,100$ ms, 0.4 $\pm$ 0.1% total closings; mean $\pm$ SEM of three recordings). In each recording, cluster boundaries are defined using the fastest resolvable type of desensitization closing. At 100 $\mu$M ACh, fast desensitization closings are readily identifiable and including them when computing cluster duration yields a mean duration of 37 $\pm$ 7 ms (mean $\pm$ SEM, $n = 3$). However, the fast and me-

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**Figure 9.** Schemes used in simulation experiments. In Schemes Ax, B1x and F3x, $k_{D_1}$, $k_{D_2}$, $k_{D_3}$, and $k_{D_4}$ (rate constants governing desensitization and recovery from desensitization), $k_{T_1}$, $k_{T_2}$, $k_{T_3}$, and $k_{T_4}$ were set to the values in Table VII. For clarity, the rate constants governing activation and block of the channel by ACh have been omitted. In the simulations, these were set to the values given in Table IV ($-70$ mV data).
medium rate desensitization closings occur primarily between activation episodes of the same channel so single channel clusters can, in principle, also be defined using the medium or slow desensitization closings. At 100 μM ACh this results in mean cluster durations of 71 ± 17 ms (medium) and 365 ± 33 ms (slow). In the presence of 10 μM tacrine and 100 μM ACh, fast desensitization closings cannot be used to define cluster boundaries because they are obscured by closings due to channel block. The medium and slow desensitization closings, however, can be readily resolved and yield clusters with mean durations of 86 ± 37 ms (medium) and 355 ± 97 ms (slow) (mean ± SEM, n = 4). These values are not significantly different from the corresponding cluster durations in the absence of tacrine (P > 0.7 by Student’s t test). The failure of tacrine to alter cluster duration is consistent with a mechanism in which the receptor can desensitize from open-blocked states at the same rate as from the open-state.

Simulation of Single Channel Data

The concentrations of tacrine used in this study give rise to closed times which overlap with closed times arising from fast and medium onset desensitization. Although desensitization closings make only minor contributions to the closed time histogram, our modelling results might be biased by their inclusion. In particular, we were concerned that (a) improvements in fit relative to the classic sequential model for channel block (Scheme B1), and that (b) the improved fits yielded by Schemes F4–I1 relative to Scheme F3 were due to contamination with desensitization closings. To address this question we simulated single channel open and closed dwell times using the method of Clay and DeFelice (1983). First we expanded Scheme A by adding two desensitized states arising from the diliganded open state (Fig. 9, Scheme Ax) and simulated single channel responses to 100 μM ACh according to the best-fit parameters for Scheme A. We then varied the rate constants governing desensitization to replicate the time constants and weights of the fast and medium rate desensitization closings in our experimental data (final values given in Table VII). Next, we incorporated the fast and medium desensitization closings in Schemes B1 and F3 assuming (a) that desensitization occurs from open or open-blocked states but not closed-states of the receptor and (b) that the binding of tacrine to the receptor did not alter the desensitization rate constants (the expanded schemes, given in Fig. 9 are denoted by the suffix x i.e., Scheme B1x, F3x).

We simulated 5,000 channel openings and closings at 1, 2, 3, 6, 10, 20, 30, and 60 μM tacrine according to Schemes B1x and F3x using the rate constants that gave the best fit of each scheme to our experimental data at −70 mV (Table VII). Next, we selected clusters of openings for analysis as described above and fitted, in turn, Schemes B1, C3, C4, E1, F2, F3, F4, G1, G2, and I1 to each data-set. The log-likelihood values for these fits are summarized in Table VIII.

Data simulated according to Scheme B1x were well described by Scheme B1 with fitted parameters within 9% of the input values. Schemes C3, E1, and F2 did not produce convergent fits to Scheme B1x data but improved fits relative to Scheme B1 were obtained with Schemes F3, F4, G1, G2, and I1. This improvement pre-

### Table VII

<table>
<thead>
<tr>
<th></th>
<th>Scheme B1x</th>
<th>Scheme F3x</th>
</tr>
</thead>
<tbody>
<tr>
<td>$k_{01}$</td>
<td>30</td>
<td>30</td>
</tr>
<tr>
<td>$k_{0-1}$</td>
<td>400</td>
<td>400</td>
</tr>
<tr>
<td>$k_{0-2}$</td>
<td>18</td>
<td>18</td>
</tr>
<tr>
<td>$k_{0-3}$</td>
<td>33</td>
<td>33</td>
</tr>
<tr>
<td>$k_{1-1}$</td>
<td>84</td>
<td>96</td>
</tr>
<tr>
<td>$k_{1-2}$</td>
<td>144</td>
<td>655</td>
</tr>
<tr>
<td>$k_{1-2}$</td>
<td>—</td>
<td>61</td>
</tr>
<tr>
<td>$k_{2-2}$</td>
<td>—</td>
<td>497</td>
</tr>
</tbody>
</table>

Data were simulated according to Schemes B1x and F3x using the method of Clay and DeFelice (1983). $k_{01}$ and $k_{0-1}$ are rate constants governing the entry of the receptor into the fast and medium duration desensitized states and $k_{0-1}$ and $k_{0-2}$ are the rate constants for exit from those states. $k_{1-1}$ and $k_{1-2}$ are the association rate constants and $k_{1-1}$ and $k_{2-2}$ are the dissociation rate constants for tacrine binding at two sites within the open channel. Values of rate constants governing desensitization were derived by iterative simulation of data according to Scheme Ax, varying the rate constants until the closed time histogram replicated our experimental data obtained at 100 mM ACh (−70 mV values). Values of $k_{1-1}$, $k_{1-2}$, $k_{1-3}$, and $k_{1-4}$ are from the maximum likelihood fits of Schemes B1 and F3 to our experimental data (−70 mV).

### Table VIII

Log-likelihood Values Derived from Scheme Fitting to Simulated Data

<table>
<thead>
<tr>
<th></th>
<th>Scheme B1x</th>
<th>Scheme F3x</th>
</tr>
</thead>
<tbody>
<tr>
<td>Scheme B1</td>
<td>235,984</td>
<td>232,928</td>
</tr>
<tr>
<td>Scheme C3</td>
<td>Did not converge</td>
<td>233,480</td>
</tr>
<tr>
<td>Scheme C4</td>
<td>235,984</td>
<td>235,069</td>
</tr>
<tr>
<td>Scheme E1</td>
<td>Did not converge</td>
<td>234,350</td>
</tr>
<tr>
<td>Scheme F2</td>
<td>Did not converge</td>
<td>234,334</td>
</tr>
<tr>
<td>Scheme F3</td>
<td>235,989</td>
<td>234,426</td>
</tr>
<tr>
<td>Scheme F4</td>
<td>235,989</td>
<td>234,436</td>
</tr>
<tr>
<td>Scheme G1</td>
<td>235,989</td>
<td>234,462</td>
</tr>
<tr>
<td>Scheme G2</td>
<td>235,989</td>
<td>234,426</td>
</tr>
<tr>
<td>Scheme I1</td>
<td>235,989</td>
<td>234,436</td>
</tr>
</tbody>
</table>

Log-likelihood values were generated by fitting schemes to data simulated using Schemes B1x and F3x. Schemes B1x and F3x incorporate two desensitized states leading from the open and open-blocked states. For each scheme, channel openings and closings were simulated for 100 μM ACh in the presence of 1–60 μM tacrine using the method of Clay and DeFelice (1983). Clusters were defined and selected for analysis as described in the text.
sumably arises because the fitting process interprets the desensitization closings in terms of the additional closed states afforded by more complex models. However, the increase in log likelihood for Schemes F3, F4, G1, G2, and I1 versus Scheme B1 was much smaller with the simulated data (five LL units) than with our experimental data (~2,000 LL units) and the fitted values for $k_{T+2}$, $k_{T+3}$ and $k_{T+4}$ were in all cases very small (<2.5 μM$^{-1}$ s$^{-1}$) with errors >50%. Further, the fitted values for $k_{T+1}$ and $k_{T-1}$ were in all cases within 15% of the corresponding input values from Scheme B1. Thus, with our experimental data, the substantial improvements in fit obtained with two-site relative to one-site models are not artifacts caused by receptor desensitization.

Similarly, fits of Scheme F3 to data generated using Scheme F3x yielded excellent agreement between the fitted parameters and the rate constants used to parameterize the scheme (maximum deviation of 4%). Relative to Scheme F3, improved fits were obtained with Schemes F4, G1, and I1 but not with Scheme G2 or any other model tested. These improvements presumably arise because the fitting process accounts for some of the desensitization closings using the additional blocked state in Schemes F4, G1, and I1. Unlike our results with Scheme B1x, however, the increases in log likelihood value with Schemes F4, G1, and I1 are of similar magnitude to improvements in fit, relative to Scheme F3, that are obtained when these schemes are fitted to our experimental data. Thus, our simulation results suggest that the likelihood values of models in which tacrine is postulated to bind randomly to two sites in the open channel or which allow for channel closing with tacrine bound, may be significantly inflated by the inclusion of desensitization closings in our data.

Scheme G2, on the other hand, does not improve fits (relative to Scheme F3) to data simulated using Scheme F3x. This indicates that for our simulated data, desensitization closings cannot be accommodated by the addition of closed-blocked states. By contrast, Scheme G2 does produce an improved fit relative to Scheme F3 with our real patch clamp data. Based on our results with simulated data, this improvement is unlikely to arise from the presence of desensitization closings and must therefore be due to dwells of the receptor in the closed-blocked state.

Voltage Dependence of Tacrine Binding

Fits of Scheme G2 to our data revealed that the dissociation constants (calculated from the fitted rate constants) for the two tacrine binding sites in the open channel decreased as the membrane potential became more hyperpolarized (Table VI). Applying the Woodhull equation (Woodhull, 1973) to these data yields electrical distances of 0.38 for the first binding site and 0.32 for the second site. Binding to the closed channel also shows apparent voltage sensitivity but inspection of the association and dissociation rate constants at this site reveals that they do not vary in a consistent manner.

DISCUSSION

Open channel block of the nAChR has classically been described by a simple sequential mechanism in which blockers bind to a single site within the open channel of the receptor (Scheme B1). For many compounds, e.g., QX-222 (Charnet et al., 1990), epibatidine (Prince and Sine, 1998a), and pyrantel (Rayes et al., 2001), such models provide a good, quantitative description of the interactions between the blocker and the nAChR channel, at least at lower concentrations of blocker. In other studies, simple sequential models have failed to explain fully the kinetics of nAChR block (Neher, 1983; Papke and Oswald, 1989; Dilger et al., 1997; Evans and Martin, 1996), but in most cases the merits of alternative models have not been explored systematically.

In our current study we found that the simple sequential model for open channel block can describe accurately the concentration-dependent decrease in channel open time produced by tacrine, but fails to account for the concentration dependence of the closed-time distribution. The simple sequential mechanism for open channel block predicts that the duration of closings due to channel block should depend solely on the dissociation rate constant of the blocker and thus should not vary with blocker concentration.

Concentration dependence of channel closings requires that tacrine stabilizes a state of the receptor in which ion flux does not occur. Thus, there are two general classes of mechanism that could explain the effect of tacrine on the open and closed time distributions. The first class requires that tacrine binds to and blocks the open channel of the nAChR, but also binds to a closed state of the receptor. The second class involves multiple binding sites for tacrine on the open state of the receptor. Below, we evaluate a variety of kinetic models within these two general frameworks.

Models Involving Interactions with Closed States

Parallel block mechanisms. The first general mechanism we examined (Mechanism C) allows tacrine to bind to the channel in both the open ($A_2O$) and closed state ($A_2C$) and allows channel gating to occur with tacrine bound (Adams, 1977). This type of mechanism has been termed “parallel block” because it provides two parallel pathways for the receptor to switch between open and closed states. In studies of fetal mouse receptors in a clonal cell line, Papke and Oswald (1989) found that parallel block provided a quantitatively better description than classic sequential block to explain the kinetics of tetracaine, phencyclidine, and N-allyl-
normetazocine on single channel currents activated by low concentrations of ACh. A similar mechanism was also proposed by Neely and Lingle (1986) to explain the kinetics of chlorisondamine block.

Our first derivative of the parallel block mechanism was Scheme C1 in which we assumed (a) that the channel could open and close at the same rate irrespective of whether tacrine was bound and (b) that the rate constants governing tacrine binding were the same in the open and closed states of the receptor. This mechanism yielded an even worse description of our data than the sequential model (Scheme B1). Next, we tested a mechanism (Scheme C2) in which the constraints on channel gating and tacrine binding were removed. However, we found that fits of Scheme C2 to our data did not yield a full, parallel block mechanism. Instead, Scheme C2 converged with values of $k_{T^{-2}}$ and $k_{T^{-2}}$ (association and dissociation rates governing tacrine binding to the closed channel) close to zero and yielded the same log-likelihood value as Scheme C3 (in which it was assumed that tacrine could not bind to the closed channel). The mechanism described by Schemes C2 and C3 has two main characteristics. First, tacrine associates only with the open state of the channel. Second, when the channel has bound tacrine it can access an additional nonconducting state from which tacrine cannot dissociate. Although Schemes C2 and C3 both yield better fits than the classic sequential model (Scheme B1, see Table V and Fig. 3) neither predicts concentration dependent block closings. It is therefore not intuitively obvious from where the improvement in fit obtained with these schemes arises (they probably work better by merely including a second closed state). Possible identities of the additional nonconducting state are discussed below in the context of two site models.

We also examined a variation of the parallel block mechanism that assumes that the channel cannot gate with tacrine bound (Scheme C4), but which allows tacrine to bind to the closed state of the receptor. In parallel block mechanisms the effective channel opening rate, $\beta^*$, will vary with tacrine concentration because the $A_2C_T$ state is connected directly to $A_2C$ and thus indirectly to AC and C. Effects on $\beta^*$ will be most pronounced when $k_{T^{-2}}$ is much faster than $\beta^*$ (channel opening rate with tacrine bound) e.g., when $\beta^*$ and $\alpha^*$ are set to zero: as the concentration of tacrine is raised the receptor will spend progressively more time shuttling between the $A_2C_T$ and $A_2C$ states. Although Scheme C4 also yielded an improved fit relative to Scheme B1, two factors suggest that this type of mechanism is unlikely. First, examination of closed time histograms (Fig. 5 A) shows that the component of the closed-time distribution attributable to $\beta^*$ (mean duration 100–200 μs) is unaffected by tacrine. Second, for $\beta^*$ to be lengthened significantly by tacrine, $[\text{tacrine}]k_{T^{-2}}$ must approach or exceed ($\beta + k_{-2}$), which for ACh at $-70$ mV is $\sim 73,000$ s$^{-1}$. Tacrine-induced closings are readily distinguishable in the closed time histogram and increase approximately linearly in duration with increasing concentration. To explain these findings at, for example, 2 μM tacrine, requires $k_{T^{-2}}$ to be $>36,000$ μM$^{-1}$ s$^{-1}$. This is $\sim 36$-fold faster than the upper limit for a diffusion-limited association reaction and thus is physically unreasonable.

**Competitive Interactions**

The second type of model we considered combines sequential open channel block with a competitive interaction at the ACh binding sites (Scheme D1). This model was of interest because ligand binding studies on human cortical nAChRs (Perry et al., 1988) and whole brain tissue (Hunter et al., 1989) provided evidence for competitive binding at neuronal nAChR ACh recognition sites, with $K_d$ values in the low micromolar range. However, more recent studies suggest a complex mode of interaction with neuronal receptors. Svensson and Nordberg (1996) and Svensson (2000) found that chronic treatment with tacrine modulates receptor number in clonal SHSY5Y and M10 cells and speculated that this may involve interaction at an allosteric site in addition to the agonist binding site. A study on α4β2 and α4β4 subunit combinations (Zwart et al., 2000), however, suggested that tacrine binds to the agonist recognition site and acts as a coagonist with ACh, in addition to blocking the receptor in the open state. Although it is not always possible to extrapolate results obtained with neuronal AChRs to the muscle receptor, competitive interactions combined with open channel block could, in theory, explain our present results. Thus, we tested the hypothesis that tacrine competes with ACh. We found three lines of evidence which together strongly suggest that tacrine does not exert its effects via a competitive mechanism. First, we fitted a model combining competitive interactions with open channel block (Scheme D1). Although this mechanism yielded a significantly better fit at all membrane potentials than the classic sequential model for open channel block, it ranked poorly compared with other mechanisms. The poor fit likely results because competitive interactions, like parallel block mechanisms, are predicted to alter the value of $\beta^*$. Second, we observed that the decrease in $P_{open}$ produced by 10 μM tacrine at 100 and 300 μM ACh was essentially the same. A competitive mechanism predicts less inhibition at higher concentrations of agonist. Finally, we performed ligand binding assays to determine directly the $K_i$ for tacrine competition against the initial rate of $[\text{[125I]I}]$-labeled α-bungarotoxin. The affinity of tacrine in this assay is 300 μM, much higher than the IC$_{50}$ value determined in patch-clamp experiments.
Multiple Block Sites

We next examined general classes of mechanism involving multiple binding sites for tacrine within the open receptor channel. The first model we examined (Scheme E1) postulates that there are two block sites at different depths within the channel. Tacrine binds first to the upper site, thereby blocking the channel, and then can either dissociate or diffuse down the channel to the deeper site. A second molecule of tacrine can then bind to the upper site, trapping the first molecule in the channel. Similar models have been used to fit data for block of nAChRs by ACh itself (Maconochie and Steinbach, 1995) as well as the anthelmintic agent, morantel (Evans and Martin, 1996). As in both of these previous studies, Scheme E1 gave superior fits to our data compared with the classic sequential scheme for open channel block (P < 0.0001 by LRT).

We also considered a general mechanism in which tacrine can associate randomly with two binding sites in the open state of the receptor (Mechanism F). To our knowledge, models involving random association at two binding sites have not been used to describe open channel block previously, but a derivative of this mechanism, in which the two sites were assumed to have very different affinities, was examined by Maconochie and Steinbach (1995) as a possible mechanism for block by ACh. The first model we tested was Scheme F1, which allows random association at the two sites and permits allosteric interactions. We found that Scheme F1 yielded excellent fits to our data with log-likelihoods 1,600–2,600 U higher than the sequential model for open channel block (P < 0.0001 by LRT). However, the fitted values for \( k_{T3}, k_{T4}, k_{T3}, \) and \( k_{T4} \) were ill-defined and very slow. This prompted us to examine three simplified versions of Scheme F1. In Scheme F2 we assumed full independence of the tacrine binding sites. This model produced significantly worse fits to our data (P < 0.0001 by LRT) than Scheme F1. Next, we assessed a model in which the state \( A_2B_T \) was eliminated (Scheme F3). Again, we found that this model did not perform as well as Scheme F1. Finally, in Scheme F4, only the transitions governed by \( k_{T14} \) and \( k_{-4} \) were eliminated. We found that this model gave equal log-likelihood values to those obtained with Scheme F1 and that the fitted parameters had much lower error estimates. The rate constants derived from fits to Scheme F4 (Table VI) describe a model in which the two unoccupied tacrine binding sites differ greatly in affinity. The binding of tacrine to the higher affinity site enhances the affinity of the remaining site, but when the low affinity site is occupied first, occupancy of the high affinity site is prevented. Thus, the two sites interact with positive cooperativity but the allosteric interaction depends on the order in which the sites become occupied. One possible physical correlate of this model would involve two binding sites at different depths within the

channel. Tacrine can interact with either site, but association with the upper site is allosterically enhanced by occupancy of the lower site. On the other hand, if the upper site is the first to bind tacrine, access to the lower site is prevented by steric hindrance. However, while consideration of log-likelihood values clearly demonstrates that Scheme F4 provides a good description of our data, our results from simulation experiments do not provide support for this model and suggest that the apparent superiority of Scheme F4 over Scheme F3 may be due to inclusion of channel closings arising from fast and medium modes of receptor desensitization.

More Complex Models

Thus far we have discussed three distinct types of kinetic model which yielded improved fits to our data relative to the sequential model: a scheme in which the channel can gate with tacrine bound, a scheme involving interactions with the diliganded closed state of the receptor and a series of models involving two binding sites on the open state of the channel. Therefore, we wished to see if combining features of these types of model into a single mechanism would yield further improvements in the description of our data. The first series of models we considered (Mechanism G, Fig. 3) extends the parallel block mechanism (Mechanism C) by adding a second binding site for tacrine in the open state of the receptor. Dilger et al. (1997) found that this type of model provided a good description of the block kinetics of pentobarbitone at the mouse fetal-type nAChR. Like tacrine, pentobarbitone produces concentration-dependent closed times. Based on our results from single-site parallel block models, we considered three schemes within this general framework. The first model we examined, Scheme G1, gave substantial improvements in fit compared with both its parent schemes (Schemes F3 and C3). This model features two binding sites for tacrine in the open channel and an additional “dead-end” state that the receptor can access when the channel has bound a single molecule of tacrine, but from which tacrine cannot dissociate. At least three physical correlates of Scheme G1 can be envisioned. First, the dead-end state may arise because the channel closes, and traps tacrine in its binding site. Second, in our modelling experiments we have assumed that the block of the channel by tacrine and ACh are mutually exclusive. However, the dead-end state in Scheme G1 might also arise because ACh binds to a site within the channel thereby preventing tacrine from escaping. Finally, the additional state in Scheme G1 might correlate with a desensitized state. We consider this the most likely explanation because in our simulation experiments, Scheme G1 gave much better fits than Scheme F3 to data generated using Scheme F3x (i.e., Scheme F3 incorporating desensitization closings). Thus, the apparently superior
fits obtained when Scheme G1 was applied to our patch-clamp data may derive from the inclusion of desensitization closings in our data.

Next, we fitted Scheme G2 to our data. This model assumes that tacrine can bind to both the open and closed states of the channel but does not permit channels occupied by tacrine to open or close. We found that Scheme G2 gave a superior fit compared with Scheme G1 at −70 and −150 mV but not at −110 mV. Finally, we examined Scheme G3, which describes a full parallel block mechanism that allows binding of tacrine to the open and closed states and permits channel gating with tacrine bound. At −70 mV and −150 mV fits of Scheme G3 yielded values of β* and α* close to zero and therefore simplified to Scheme G2. Conversely, when Scheme G3 was fitted to our −110 mV data it yielded parameter values of kT-3 close to zero and simplified to Scheme G1. Thus, consistent with our results from single site models, our data do not appear to be compatible with parallel block mechanisms.

Within the framework of Mechanism G, Scheme G2 produced the best fit to two out of our three datasets. Therefore, we used Scheme G2 as the starting point for our final two models. First we expanded Scheme G2 to allow binding of tacrine to two sites on the closed receptor (Scheme H1). Addition of the extra closed-state binding site did not, however, produce any significant improvements in the fits. Finally, we examined Scheme I1, which combines Schemes G2 and F3, allowing tacrine to bind randomly to two sites in the open channel and to interact with a single site on the closed state of the receptor. Overall, Scheme I1 gave the highest log-likelihood values of any model tested in this study. However, as with Schemes F3 and G1, the results of our simulations suggest that the improvements generated by the incorporation of the A_2B state are most likely due to the inclusion of desensitization closings in our data.

Our simulated data reveal that fits to models which postulate the binding of tacrine to closed as well as open states (Scheme G2) do not appear to be greatly influenced by desensitization closings, unlike models in which tacrine can bind randomly to two sites within the channel (Schemes F1, F4, I1) or which contain “dead-end” states (Scheme G1). Assuming that this finding can be extrapolated to our experimental data, the model that provides the best, unbiased description of our data is therefore Scheme G2. A simple interpretation of Scheme G2 is a mechanism in which there are two allosterically coupled binding sites for tacrine within the channel. One of these binding sites is accessible to tacrine in the closed as well as the open state of the channel, but the second site can be occupied only when the channel is open and tacrine has bound to the first site.

Nature and Location of the Tacrine Binding Sites

Conformation of the “blocked” state. Thus far we have assumed that the “blocked” states in our models arise from the physical plugging of the channel by tacrine. However, many noncompetitive inhibitors of the nAChR have also been reported to cause receptor desensitization as well as channel block (Benoit and Changeux, 1993; Arias, 1996) and distinguishing between these modes of inhibition is problematic (Clapham and Neher, 1984). It is therefore possible that tacrine may have a similar dual action i.e., that one or both of the “blocked” states in Scheme G2 are in fact new desensitized states induced by tacrine. From our modelling data, we cannot distinguish between channel block and desensitization because our models identify states by only connectivity and conductance i.e., a “blocked” state is identified as a nonconducting state that the channel enters when tacrine binds and this description applies equally well to a desensitized state.

However, three lines of evidence presented in this paper point toward a site of action within the channel lumen and argue against tacrine affecting receptor desensitization: First, our binding studies demonstrate that tacrine does not cause receptor desensitization: at the concentrations used in this study it acts solely as a low potency competitive antagonist (Ki 300 μM). Second, the actions of tacrine are voltage dependent, suggesting a site of action within the membrane field. Similar to our observations with tacrine, a study with chlorpromazine by Benoit and Changeux (1993) found that its desensitizing actions were insensitive to membrane potential, whereas its channel blocking actions were voltage sensitive. Finally, tacrine does not affect cluster duration. Cluster duration is inversely proportional to the desensitization rate of the receptor (Sakmann et al., 1980; Auertbach and Akk, 1998). However, these findings leave open the possibility that tacrine stabilizes or induces a short-lived desensitized state that does not alter agonist affinity in ligand binding studies. A similar mechanism was proposed recently to explain the actions of the quinacrine at the mouse adult nAChR (Spitzmaul et al., 2001).

Location of the tacrine binding sites. Apparent electrical distances derived from the Woodhull equation (Woodhull, 1973) have been used extensively to infer the locations of blocker binding sites within ion channels. Assuming that the field drops linearly across the membrane, our data suggest (a) that both tacrine binding sites are located at similar depths in the open channel and (b) that the sites with which tacrine’s amino group interacts are located about one third of the way down the channel. This is similar to the electrical distance calculated for quinacrine (Adams and Feltz, 1980). By contrast, the classic open channel blocker QX-222 binds at an electrical distance of ~0.8 (Neher
creased with increasing hyperpolarization (e- previously in terms of channel gating and channel block reveal broadly similar behavior to nAChRs characterized voltage dependence of human adult nAChR kinetics, re-
to the best of our knowledge are the first to examine the block of the receptor by ACh. These experiments, which produce dramatic changes in agonist affinity. We spec-
ulate that in human adult nAChRs, the structural ma-
chinery that couples agonist binding to channel gat-
ing and desensitization may also couple the agonist binding sites to an element within the membrane field that senses the potential difference across the cell membrane.

**Comparison of the Maximum Likelihood Method with Other Methods of Analyzing Block**

Previous single channel studies of nAChR channel block for the most part, have examined the effects of
blocks on parameters such as open, burst, and block duration and blocking frequency. These types of analysis can yield results that are difficult to interpret mechanistically and have only limited sensitivity in terms of their abilities to discriminate between kinetic models. For example, models E1–F4, G2, H1, and H2 each predict linear relationships between tacrine concentration and 1/\(\tau_{\text{app}}\), constant open-time per burst, an increase in burst duration, and concentration dependence of the block-closed time.

To the best of our knowledge, the present study is the first heuristic study of nAChR channel block to make use of maximum likelihood scheme fitting to single channel data. In contrast with previous methods, maximum likelihood fitting offers the ability to discriminate between even very closely related kinetic schemes. The main drawbacks of the maximum likelihood method are that (a) it requires detailed knowledge of the parameters governing agonist interactions with the receptor and (b) it requires the use of agonist concentrations that produce clearly defined clusters, i.e., concentrations that produce significant levels of desensitization. However, these limitations can be overcome with appropriate controls and our present results indicate that maximum likelihood fitting is a sensitive and robust technique for analysis of channel block.

In summary, this study demonstrates that the kinetics of tacrine cannot be explained by the classic sequential model for open channel block and are instead consistent with a model in which tacrine binds to two sites within the open channel and to a single site on the closed channel. Our results underline the complexity of channel block at the nAChR and suggest that our picture of open channel block of the receptor may require revision.

**APPENDIX A**

The classic sequential mechanism for open channel block (Fig. 3, Scheme B1) has simple connectivity and predicts a linear relationship between the reciprocal of the mean channel open duration (\(\tau_{\text{open}}\)) and the concentration of open channel blocker (\(T\)):

\[
\frac{1}{\tau_{\text{open}}} = \alpha + T.k_{T+1},
\]

where \(\alpha\) is the channel closing rate and \(k_{T+1}\) is the association rate for tacrine.

Plots of Eq. A1 can be used to derive values of \(\alpha\) and \(k_{T+1}\), but it is first necessary to correct apparent mean open durations for unresolved dwells in the closed states. These missed closings result in the concatenation of successive channel openings and thus in overestimation of \(\tau_{\text{open}}\). In the present study, however, this correction is not possible because the partially resolved brief closings that arise from channel gating are of a similar duration to those that arise from block of the channel by ACh itself. Below we demonstrate that for our present data, open time correction is unnecessary and that plots of reciprocal apparent mean open time (\(\tau_{\text{app}}\)) against tacrine concentration also yield a straight-line with a slope approximating \(k_{T+1}\).

**Closed Time Distribution for Scheme B1**

Scheme B1 predicts three exponential components in the closed time histogram due to entry of the channel into the “C” states (C, AC and A2C). We term these components “fast,” “medium” and “slow,” but it is important to realize that the mean durations of these components vary with agonist concentration.

As the C, AC, and A2C states are interconnected, the rate constants (\(\lambda_f, \lambda_m, \lambda_s\)) and relative areas (\(a_f, a_m, a_s\)) of the fast, medium, and slow exponential components do not relate in a straightforward manner to individual rate constants in Scheme B1 (The definitions of the rate constants and concentration symbols used in Scheme B1 are set out in the main body of this paper [Fig. 3]), and must be derived by solving a cubic function. The derivation of this function closely follows the method used by Colquhoun and Hawkes (1981) for the allosteric agonist mechanism (defined as mechanism 3.1 in their paper) and will not be repeated here. In Table IX we set out the values of the rate constants and relative areas at 100 \(\mu M\) ACh (–70 mV) calculated using the parameters for ACh activation in Table IV.

Once the rate constants and relative areas of the fast, medium and slow components are known, one can readily calculate the relative fraction of closings in each component (\(F_f, F_m, \) and \(F_s\), respectively) that is resolved given a dead-time of \(r\).

<table>
<thead>
<tr>
<th>Membrane Potential</th>
<th>(-70) mV</th>
<th>(-110) mV</th>
<th>(-150) mV</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\lambda_f) (s(^{-1}))</td>
<td>79,317</td>
<td>71,697</td>
<td>70,352</td>
</tr>
<tr>
<td>(\lambda_m) (s(^{-1}))</td>
<td>27,337</td>
<td>19,774</td>
<td>18,384</td>
</tr>
<tr>
<td>(\lambda_s) (s(^{-1}))</td>
<td>8,543</td>
<td>7,978</td>
<td>8,506</td>
</tr>
<tr>
<td>(a_f)</td>
<td>0.61</td>
<td>0.71</td>
<td>0.78</td>
</tr>
<tr>
<td>(a_m)</td>
<td>0.09</td>
<td>0.11</td>
<td>0.08</td>
</tr>
<tr>
<td>(a_s)</td>
<td>0.3</td>
<td>0.18</td>
<td>0.14</td>
</tr>
<tr>
<td>(Z_f)</td>
<td>0.17</td>
<td>0.26</td>
<td>0.34</td>
</tr>
<tr>
<td>(Z_m)</td>
<td>0.07</td>
<td>0.14</td>
<td>0.14</td>
</tr>
<tr>
<td>(Z_s)</td>
<td>0.76</td>
<td>0.6</td>
<td>0.52</td>
</tr>
</tbody>
</table>

The rate constants (\(\lambda\)) and relative areas (\(a\)) of the fast, medium, and slow exponential components of the unblocked closed state p.d.f were calculated at a concentration of 100 \(\mu M\) ACh as described by Colquhoun and Hawkes (1981). The relative contribution to the total time encompassed by the p.d.f (\(Z\)) was calculated using Eq. A4.
Thus, the fraction \((F_c)\) of all resolved closed intervals is given by:

\[
F_c = a_f F_f + a_m F_m + a_r F_r,
\]

and the apparent closing rate of the channel

\[
\alpha_a = F_c/\alpha.
\]

Similarly, the fraction of closings due to ACh block that is resolved \((F_{ACh})\) is

\[
F_{ACh} = e^{-r_{kB-1}},
\]

and the apparent blocking rate for ACh \((k_{BA})\) is

\[
k_{BA} = F_{ACh} r_{kB+1}.
\]

Assuming, further, that all closings due to tacrine block are resolved, an expression for the total time spent in A2O \((\tau)\) within a resolved opening is therefore:

\[
\tau_i = \frac{1}{\alpha_a + A_i k_{BA} + T_i k_{T+1}}.
\]

However, resolved openings also contain a finite contribution \((\tau_u)\) from unresolved closings and ACh block closings. Therefore the total mean duration of an apparent opening \((\tau_{app})\) is:

\[
\tau_{app} = \frac{1}{\alpha_a + A_i k_{BA} + T_i k_{T+1}} + \tau_u
\]

and

\[
\frac{1}{\tau_{app}} = \frac{\alpha_a + A_i k_{BA} + T_i k_{T+1}}{1 + \tau_u(\alpha_a + A_i k_{BA} + T_i k_{T+1})}.
\]

Thus, when \(\tau_u\) is small compared with the total time spent in A2O \((\tau_i)\), the reciprocal of the mean apparent open time will be linearly related to the concentration of tacrine:

\[
\frac{1}{\tau_{app}} = \frac{1}{\tau_i} = \alpha_a + A_i k_{BA} + T_i k_{T+1} = \frac{1}{\tau_0} + T_i k_{T+1}, \quad (A3)
\]

where \(\tau_0\) is the apparent mean open time in the absence of tacrine. This is a useful general result because it allows the estimation of blocker association rates at high concentrations of agonist i.e., under conditions where rates of opening of the channel and block of the channel by the agonist compromises distort the true channel open time.

**Estimation of the Error Magnitude for Scheme G2**

Scheme G2 (Fig. 3) also predicts that apparent open time obeys Eq. A3. Thus, the errors involved in applying Eq. A3 to our data can be estimated from our derived rate constants for Scheme G2. The first step in this calculation requires us to determine the equilibrium occupancy of A2O \((E_{O})\), the unresolved fraction of the equilibrium occupancy of A2B \((E_{Bu})\), and the fraction of the “C” closed states that is unresolved \((E_{Cu})\). \(E_{O}\) and \(E_{Bu}\) are relatively straightforward:

\[
E_O = \frac{A_2 O}{A_2 O + A_2 B + C_{total} + T_{total}}
\]

\[
E_{Bu} = \frac{A_2 B A \pi}{A_2 O + A_2 B + C_{total} + T_{total}},
\]

where:

\[
C_{total} = C + A C + A_2 C = C + \frac{C A^2}{K_1 K_2}
\]

\[
A_2 O = \frac{C \theta A^2}{K_1 K_2}
\]

\[
A_2 B A = \frac{C A^2 \theta}{K_1 K_2 K_{BA}}
\]

\[
T_{total} = \frac{A_2 O T}{K_{T1}} + \frac{A_2 O T^2}{K_{T2} K_{T1}} + \frac{A_2 C T}{K_{T3}}
\]

\[
\pi = k_{B-1} \int_0^r e^{-r_{kB-1}} dt
\]

and \(\theta\) is the equilibrium constant for channel gating, \(K_{T1},\ K_{T2}\) and \(K_{BA}\) are equilibrium dissociation constants for ACh at the low and high affinity agonist binding sites and the channel block site respectively, \(C_{total}\) and \(T_{Total}\) are occupancy functions for the closed- and blocked-states respectively, and \(\pi\) is the proportion of time missed.

The use of \(\pi\) rather than the more familiar fractional number of closings is important because a given number of closings with durations less than the dead-time will distort the apparent open time less than the same number of closings with durations greater than the dead-time.

Calculation of \(E_{Cu}\) requires a little more work because the rate constants and areas of the relevant exponential components in the closed time histogram do not relate to individual states of the receptor. Our first task is to calculate the equilibrium occupancy of the “C” closed states \((E_{Cu})\).
For each of the three “C” closed state exponentials,1 we must then calculate the proportion (πₙ) of the total unresolved time encompassed by that exponential.

\[ \pi_f = \lambda_f \int_0^r e^{-\lambda_f t} dt \]

\[ \pi_m = \lambda_m \int_0^r e^{-\lambda_m t} dt \]

\[ \pi_s = \lambda_s \int_0^r e^{-\lambda_s t} dt \]

and the fractional contribution (Zₙ) of each component to the total time spent in the closed state:

\[ Z_f = \frac{\frac{a_f}{\lambda_f}}{\frac{a_f}{\lambda_f} + \frac{a_i}{\lambda_i}} \]

\[ Z_m = \frac{\frac{a_m}{\lambda_m}}{\frac{a_f}{\lambda_f} + \frac{a_m}{\lambda_m} + \frac{a_i}{\lambda_i}} \]

\[ Z_s = \frac{\frac{a_s}{\lambda_s}}{\frac{a_f}{\lambda_f} + \frac{a_s}{\lambda_s}} \]

The unresolved occupancy of the “C” closed states is then given by:

\[ E_{Cu} = E_c(\pi_f, Z_f + \pi_m, Z_m + \pi_s, Z_s) \]

From these equilibrium occupancy functions we can calculate the ratio \( \tau_u/\tau_i \):

\[ \frac{\tau_u}{\tau_i} = \frac{E_{Cu} + E_{Bu}}{E_o} \]

At 100 \( \mu M \) ACh, this expression yields values of \( \tau_u/\tau_i \) of 0.027 at -70 mV, 0.048 at -110 mV, and 0.054 at -150 mV. These values are, as expected, independent of tacrine concentration.

Since:

\[ \tau_{app} = \tau + \tau_u = \tau_i \left( 1 + \frac{\tau_u}{\tau_i} \right) \]

then from Eq. A2:

\[ \tau_{app} = \frac{1 + \frac{\tau_u}{\tau_i}}{\alpha_a + [A] k_{Bu} + T_k_{T+1}} \]  

(A5)

From Eq. A5 it follows that:

\[ \frac{1}{\tau_{app}} = \frac{a_u + A_k_{Bu} + T_k_{T+1}}{1 + \frac{\tau_u}{\tau_i}} \]  

(A6)

Substituting our calculated values of \( \tau_u/\tau_i \) into Eq. A6 reveals that using Eq. A3 with our data generates a maximum error of 5% in \( k_{T+1} \). Thus, the calculations presented in this appendix demonstrate that correction of open times for missed gating and block events is unnecessary with our present data, and that plots of reciprocal apparent open time against tacrine concentration provide accurate estimates of \( k_{T+1} \).

APPENDIX B

In Fig. 8, we plot the predicted rate constants and relative areas of the closed-time components arising from channel block. Below, we provide a derivation of the equations used to calculate these parameters.

In Scheme G2, states A₂BT and A₂BT are connected to each other but not to any further closed states. The rate constants and relative areas of the exponentials corresponding to dwells in these two states can therefore be described using the following simplified scheme (state and rate constant definitions are as defined for Scheme G2 in the legend to Fig. 3).

(SCHEME I)

<table>
<thead>
<tr>
<th>( A_0 )</th>
<th>( A_1 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>k(_{T+1})</td>
<td>k(_{T+2})</td>
</tr>
<tr>
<td>( A_2 )</td>
<td>( A_3 )</td>
</tr>
<tr>
<td>k(_{T-1})</td>
<td>k(_{T-2})</td>
</tr>
<tr>
<td>( A_4 )</td>
<td>( A_5 )</td>
</tr>
<tr>
<td>k(_{T+1})</td>
<td>k(_{T+2})</td>
</tr>
</tbody>
</table>

Scheme I predicts a double exponential closed-time distribution with a p.d.f. of the form:

\[ f(t) = a_1 \lambda_1 e^{-\lambda_1 t} + a_2 \lambda_2 e^{-\lambda_2 t}, \]

where \( \lambda_1 \) and \( \lambda_2 \) are the rate constants of the two exponential components and \( a_1 \) and \( a_2 \) are the relative areas under the p.d.f. accounted for by \( \lambda_1 \) and \( \lambda_2 \). Note that \( a_1 \) and \( a_2 \) predict the areas of the exponentials corresponding to open channel block relative to each other in Scheme G2 but do not give information about the areas of these components relative to those of other closed states.

The transition rate matrix for Scheme I is:

\[
Q = \begin{bmatrix}
1 & 2 & 3 \\
-(k_{T-1} + k_{T+2}) & k_{T+2} & T \\
T & -k_{T-2} & 0 \\
3 & T_{k_{T+1}} & 0 & -T_{k_{T+1}}
\end{bmatrix}
\]

1In theory, the p.d.f for Scheme G2 should have four exponential components that arise from “C” closed states. The additional component is due to the closed blocked state. However, the closed blocked state has very low equilibrium occupancy and the rate constants connecting it to A₂C are slow compared with \( k_2 \) and \( \beta \). Thus, the three component model used here should be a good approximation of reality.
Defining state A as the compound closed state and state B as the open state, the appropriate partition of Q is:

\[
Q = \begin{bmatrix} Q_{AA} & Q_{AB} \\ Q_{BA} & Q_{BB} \end{bmatrix} = \begin{bmatrix} (k_{T-1} + k_{T+2}T) & k_{T-1} \\ k_{T-2} & 0 \\ T.k_{T+1} & 0 \end{bmatrix}
\]

Following the method of Colquhoun and Hawkes (1981), the Laplace transform of the p.d.f. of the closed time distribution is:

\[
f_{13}^* = \frac{k_{T-1}(s + k_{T-2})}{(s + \lambda_1)(s + \lambda_2)}. \quad (A7)
\]

Inversion of Eq. A7 yields the required p.d.f.:

\[
f_{13} = \frac{k_{T-1}(k_{T-2} - \lambda_1)\lambda_1 e^{-\lambda_1 t} + k_{T-1}(\lambda_2 - k_{T-2})\lambda_2 e^{-\lambda_2 t}}{\lambda_1(\lambda_2 - \lambda_1)} \quad (A8)
\]

The two rate constants \(\lambda_1\) and \(\lambda_2\) can then be found by solving the quadratic equation,

\[
a\lambda^2 + b\lambda + c = 0,
\]

where

\[
a = 1,
b = -\lambda_1 + \lambda_2 = k_{T-1} + k_{T-2} + k_{T+2}T,
c = \lambda_1\lambda_2 = k_{T-1}k_{T-2}
\]

Using the familiar solution:

\[
\lambda_1, \lambda_2 = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}
\]

\[
\lambda_1 = \frac{k_{T-1} + k_{T-2} + k_{T+2}T + \sqrt{(k_{T-1} + k_{T-2} + k_{T+2}T)^2 - 4k_{T-1}k_{T-2}}}{2}, \quad (A10)
\]

\[
\lambda_2 = \frac{k_{T-1} + k_{T-2} + k_{T+2}T - \sqrt{(k_{T-1} + k_{T-2} + k_{T+2}T)^2 - 4k_{T-1}k_{T-2}}}{2}, \quad (A11)
\]

As expected, the rate constants and weights of the exponential components making up the block closed-time p.d.f. do not relate directly to individual states or transitions with the kinetic mechanism, so it is difficult to make intuitive predictions about how the closed-time distribution will vary with tacrine concentration. However, insight into the kinetics described by this model can be gained by examining its behavior under conditions of limiting low and high concentrations of tacrine.

**Low Tacrine Concentration**

At limiting low concentrations of tacrine, Eqs. A10 and A11 give:

\[
\lambda_1 = k_{T-1} \quad \text{and} \quad \lambda_2 = k_{T-2}.
\]

From Eqs. A8 and A9:

\[
a_1 = \frac{k_{T-1}(k_{T-2} - \lambda_1)}{\lambda_1(\lambda_2 - \lambda_1)} \quad a_2 = \frac{k_{T-1}(\lambda_2 - k_{T-2})}{\lambda_2(\lambda_2 - \lambda_1)} \quad (A12)
\]

and \(a_1 + a_2 = 1\).

Substituting values of \(\lambda_1 = k_{T-1}\) and \(\lambda_2 = k_{T-2}\) into Eq. A12 yields \(a_1 = 1\) and \(a_2 = 0\). Thus, at very low concentrations of agonist, tacrine interacts solely with one binding site and Scheme G2 is indistinguishable from Scheme B1, the simple sequential mechanism for channel block.

**High Tacrine Concentration**

At high concentrations of tacrine, \(b^2 \gg 4ac\) and \(k_{T+1}.T \gg k_{T-1} + k_{T-2}\). Thus, from Eq. A10 we can approximate the faster rate constant, \(\lambda_f\):

\[
\lambda_f = -b = T.k_T. \quad (A13)
\]

The behavior of the slower rate constant, \(\lambda_s\), is more conveniently examined using an alternative solution to the quadratic equation:

\[
\lambda_1, \lambda_2 = \frac{2c}{-b \pm \sqrt{b^2 - 4ac}}. \quad (A14)
\]

Again assuming that \(b^2 \gg 4ac\) and \(k_{T+1}.T \gg k_{T-1} + k_{T-2}\), Eq. A14 yields the following approximation for \(\lambda_s\):

\[
\lambda_s = \frac{-c}{b} = \frac{k_{T-1}.k_{T-2}}{k_{T+2}.T}. \quad (A15)
\]

The assumptions set out above also allow us to examine the behavior of the relative areas, \(a_1\) and \(a_2\), of the two p.d.f. components. From Eqs. A13 and A15, \(\lambda_f \gg \lambda_s\). Combining this with Eq. A12 therefore yields:

\[
a_1 = \frac{k_{T-1}}{\lambda_1} = \frac{k_{T-1}}{T.k_{T+1}} \quad \text{and} \quad a_2 = 1 - \frac{k_{T-1}}{T.k_{T+1}}.
\]

Thus, at high concentrations of tacrine, the mean duration and relative area of the exponential component governed by \(\lambda_1\) and \(a_1\) will both be inversely proportional to tacrine concentration. Conversely, there will be a linear relationship between the mean duration of the component of block closings governed by \(\lambda_2\) and \(a_2\).
and tacrine concentration and the area of this component relative to $a_1$ will tend toward unity.

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